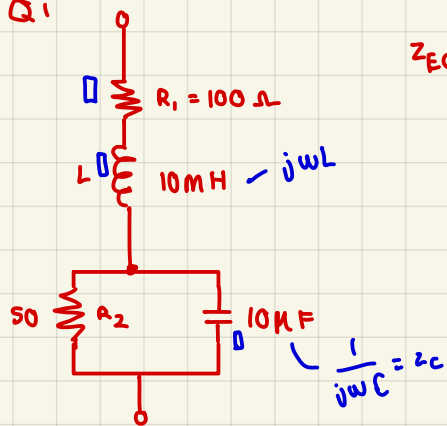


Q1



$$Z_{EQ} = Z_{R1} + Z_L + Z_{R2} // Z_C$$

$$= 100 + j(10^4)(10)(10^{-3}) +$$

$$= 100 + j100 + \frac{50}{26} - j \frac{250}{26}$$

$$= 101.9 + j90.88$$

$$Z_R + Z_L + Z_{R2} // Z_C$$

$$\frac{Z_{R2} Z_C}{Z_{R2} + Z_C}$$

$$\frac{R_2 \frac{1}{j\omega C}}{R_2 + \frac{1}{j\omega C}}$$

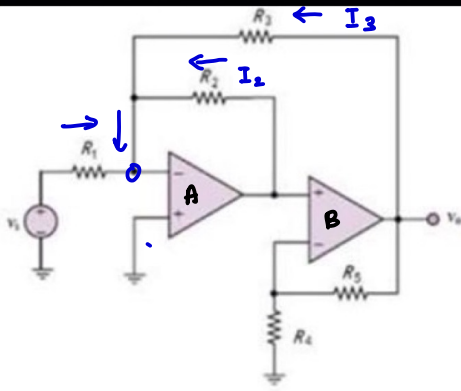
$$\frac{R_2}{j\omega C R_2 + 1}$$

$$= \frac{50}{j(10^4)(10 \times 10^{-6})(50) + 1}$$

$$= \frac{50}{j5 + 1} \frac{(1 - j5)}{(1 - j5)}$$

$$= \frac{50 - j250}{1 + 25}$$

$$= \frac{50}{26} - j \frac{250}{26}$$



$$V_s = R_1 I_1$$

$$V^+ = V^- = 0$$

$$I^+ = I^- = 0 = I_{in}$$

Given $R_1=10\Omega$, $R_2=10\Omega$, $R_3=10\Omega$, $R_4=10\Omega$ and $R_5=30\Omega$.

- ☐ $A_v = -2.25(V/V)$
- ☐ $A_v = 0.80(V/V)$
- ☒ $A_v = -0.80(V/V)$
- ☐ $A_v = 2.25(V/V)$

$$V^+ = V^- = 0$$

KCL @ -ve A node:

$$I_s + I_{F1} + I_{R2} = 0$$

$$\frac{V_s - V^-}{R_1} + \frac{V_B^+ - V^-}{R_2} + \frac{V_o - V^-}{R_3} = 0$$

$$\frac{V_s}{R_1} + \frac{V_B^+}{R_2} + \frac{V_o}{R_3} = 0$$

$$V_B^+ = \left[-\frac{V_s}{R_1} - \frac{V_o}{R_3} \right] R_2$$

KCL @ -ve B Node:

$$I_s + I_F = 0$$

$$\frac{0 - V_B^-}{R_4} + \frac{V_o - V_B^-}{R_5} = 0$$

$$-\frac{V_B^-}{R_4} + \frac{V_o - V_B^-}{R_5} = 0$$

$$V_B^- \left(\frac{1}{R_4} + \frac{1}{R_5} \right) = \frac{V_o}{R_5} \Rightarrow \frac{R_4 R_5}{R_4 + R_5}$$

$$V_B^- = V_o \left(\frac{\frac{1}{R_5}}{\frac{1}{R_4} + \frac{1}{R_5}} \right)$$

$$= V_o \left(\frac{R_4}{R_4 + R_5} \right)$$

$$V_B^+ = V_B^-$$

$$\left[-\frac{V_s}{R_1} - \frac{V_o}{R_3} \right] R_2 = V_o \left(\frac{R_4}{R_4 + R_5} \right)$$

$$-\frac{V_s R_2}{R_1} - \frac{V_o R_2}{R_3} = \frac{V_o R_4}{R_4 + R_5}$$

$$\frac{V_o R_4}{R_4 + R_5} + \frac{V_o R_2}{R_3} = -\frac{V_s R_2}{R_1}$$

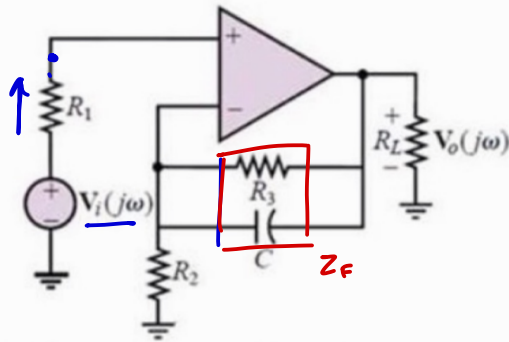
$$V_o \left(\frac{R_4}{R_4 + R_5} + \frac{R_2}{R_3} \right) = -V_s \frac{R_2}{R_1}$$

$$\frac{V_o}{V_s} = -\frac{R_2}{R_1} \div \left(\frac{R_4}{R_4 + R_5} + \frac{R_2}{R_3} \right)$$

$$= -1 \frac{1}{1} \frac{5}{4}$$

$$= -0.8$$

The circuit shown in the figure is an active filter with. Determine the cutoff frequency (ω_0) and pass-band gain (A_v) of the filter.



Given $R_1=2k\Omega, R_2=5k\Omega, R_3=50k\Omega, C=100nF$.

- ☐ $\omega_0 = 2000 \text{ rad/sec}; A_v = 8.22 \text{ dB}$.
- ☒ $\omega_0 = 200 \text{ rad/sec}; A_v = 20.83 \text{ dB}$.
- ☐ $\omega_0 = 2000 \text{ rad/sec}; A_v = 20.83 \text{ dB}$.
- ☐ $\omega_0 = 200 \text{ rad/sec}; A_v = 8.22 \text{ dB}$.

$$\begin{aligned}
 Z_F &= R_3 \parallel C \\
 &= \frac{R_3 \cdot \frac{1}{j\omega C}}{R_3 + \frac{1}{j\omega C}} \\
 &= \frac{R_3}{j\omega C R_3 + 1}
 \end{aligned}$$

$$V^+ = V_i \quad i^+ = i^- = 0$$

$$\omega = \frac{1}{R_F C_F} = 200 \text{ rad/s}$$

KCL @ Negative Node :

$$I_F + I_2 = 0$$

$$\frac{V_o - V_i}{Z_F} + \frac{0 - V_i}{R_2} = 0$$

$$\frac{V_o - V_i}{Z_F} - \frac{V_i}{R_2} = 0$$

$$\frac{V_o}{Z_F} = \frac{V_i}{Z_F} + \frac{V_i}{R_2}$$

$$\begin{aligned}
 H = \frac{V_o}{V_i} &= 1 + \frac{Z_F}{R_2} \\
 &= 1 + \frac{R_3}{j\omega C R_3 + 1} = 1 + \frac{R_3}{(j\omega C R_3 + 1) R_2} \\
 &= 1 + \frac{R_3}{R_2} \left(\frac{1}{j\omega C R_3 + 1} \right)
 \end{aligned}$$

$$\begin{aligned}
 \omega \rightarrow 0, \quad H &= 1 + \frac{R_3}{R_2} \\
 \omega \rightarrow \infty, \quad H &= 1
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} \omega \rightarrow 0 \\ \omega \rightarrow \infty \end{aligned}} \right\} \text{Test 2 condition}$$

$$\begin{aligned}
 A_v &= 20 \lg \left(1 + \frac{50}{5} \right) \\
 &= 20.83
 \end{aligned}$$

