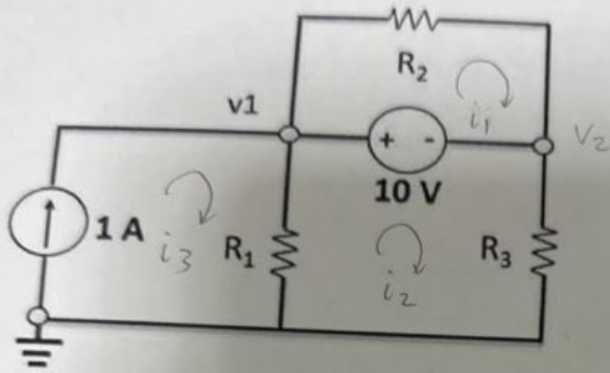



Question 1



In the circuit below, what is the node voltage v_1 ?

Given $R_1 = R_2 = R_3 = 110 \Omega$



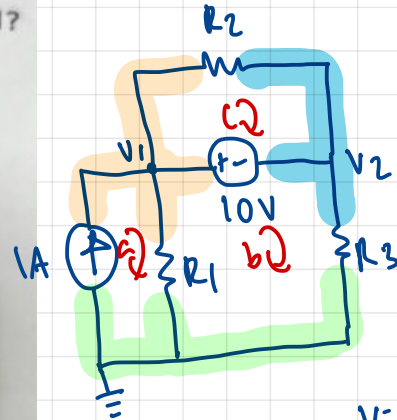
Selected Answer: 60.0 V

Answers: 65.0 V

30.0 V

35.0 V

60.0 V



$V = IR$

mesh a: 1A

$$\text{mesh b: } (1 - 1A)R_1 + 1A(R_3) = -10$$

$$1A R_1 - R_1 + R_3 1A = -10$$

$$110 1A - 110 + 110 1A = -10$$

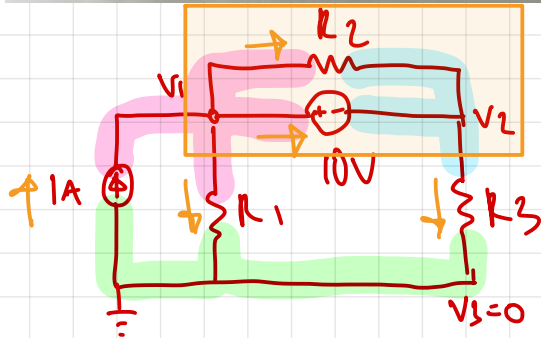
$$220 1A = 100$$

$$1A = 0.4545$$

$$V_1 - V_2 = 10$$

$$V_2 = (0.4545)(110) = 50$$

$$V_1 = 50 + 10 = 60$$



$V = IR$

$$I = \frac{V}{R}$$

node voltage method:

$$1 = \frac{V_1}{R_1} + \frac{V_2}{R_3}$$

$$110 = V_1 + V_2 \quad \text{--- (1)}$$

$$V_1 - V_2 = 10$$

$$V_1 = 10 + V_2 \quad \text{--- (2)}$$

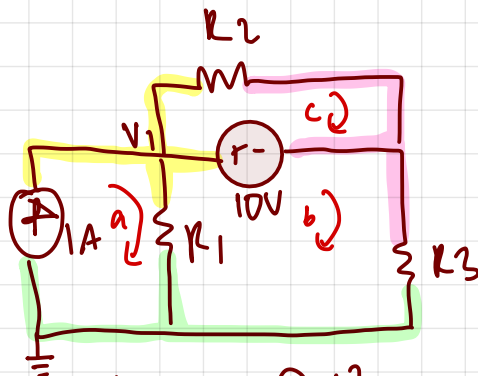
Sub (2) into (1)

$$110 = 10 + V_2 + V_2$$

$$2V_2 = 100$$

$$V_2 = 50$$

$$V_1 = 10 + 50 = 60$$



$V = IR$

node voltage @ 1?

mesh a: 1A

$$\text{mesh b: } (R_1)(i_b - 1) + R_3(i_b) = -10$$

$$110 i_b - 110 + 110 i_b = -10$$

$$220 i_b = 100$$

$$i_b = 0.4545$$

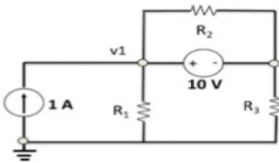
$$V_1 = (1A - i_b)(R_1)$$

$$= (1 - 0.4545)(110)$$

$$= 60$$

Question 5

In the circuit below, what is the node voltage v_1 ?
Given $R_1 = R_2 = R_3 = 30 \Omega$



Selected Answer: 20.0 V

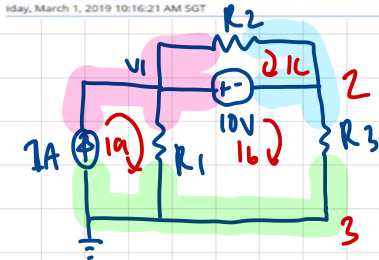
Answers:

40.0 V

30.0 V

10.0 V

20.0 V



using mesh current:

mesh $a = 1$

$$\text{mesh } b = (i_b - i_a)R_1 + i_b(R_2 + R_3) = -10$$

$$(i_b - 1)(30) + i_b(30) = -10$$

$$30i_b - 30 + 30i_b = -10$$

$$60i_b = 20$$

$$i_b = \frac{20}{60} = \frac{1}{3}$$

$$v_1 - v_2 = 10$$

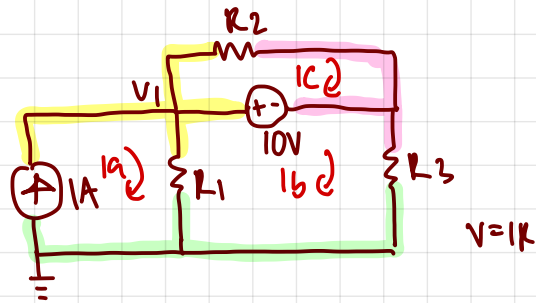
$$v_1 - 10 = 10$$

$$v_1 = 20V_{||}$$

$$v = iR$$

$$v = \frac{1}{3}(30)$$

$$= 10$$



$$i_a = 1A$$

$$i_b : -10 = (i_b - i_a)R_1 + (i_b)R_2$$

$$-10 = (i_b - 1)(30) + i_b(30)$$

$$-10 = 30i_b - 30 + 30i_b$$

$$20 = 60i_b$$

$$i_b = \frac{1}{3}$$

$$v_1 = (1 - \frac{1}{3})(30) = 20V_{||}$$

OR!

$$v_b = \frac{1}{3}(30) = 10$$

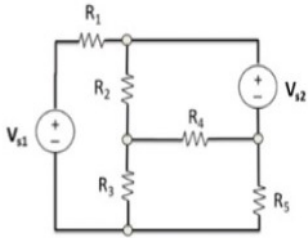
$$v_1 - v_3 = 10$$

$$v_1 - 10 = 10$$

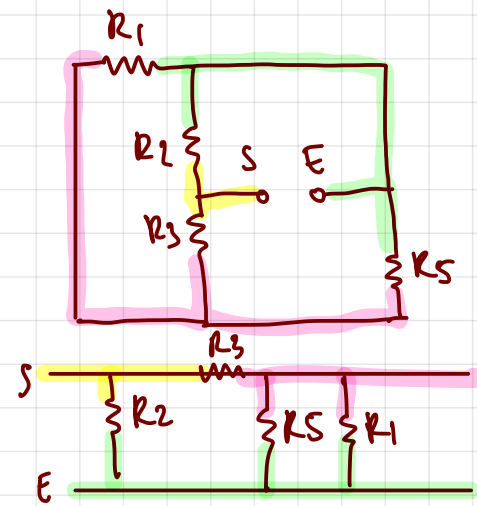
$$v_1 = 20V_{||}$$

What's the equivalent resistance seen by R_4 in the following circuit? (Hint: short circuit V_{s1} and V_{s2})

Given $R_1 = R_2 = R_3 = R_4 = R_5 = 14 \Omega$



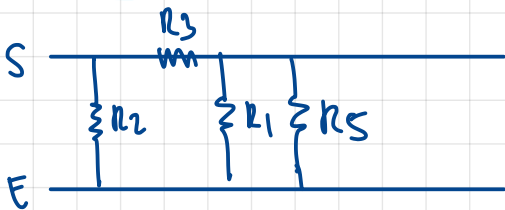
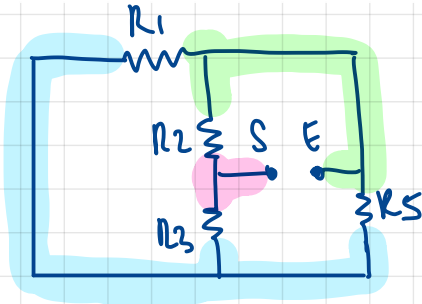
- 9.4 Ω
- 7.4 Ω
- 6.4 Ω
- 8.4 Ω



$$R_{eq1} = R_5 // R_1 = \frac{1}{\frac{1}{14} + \frac{1}{14}} = 7$$

$$R_{eq2} = R_{eq1} + R_3 = 7 + 14 = 21$$

$$R_{eq2} // R_2 = \frac{1}{\frac{1}{21} + \frac{1}{14}} = 8.4$$



$$R_{eq1} = R_1 // R_5 = \frac{1}{\frac{1}{14} + \frac{1}{14}} = 7$$

$$R_{eq2} = R_{eq1} + R_3 = 7 + 14 = 21$$

$$R_{eq2} // R_2 = \frac{1}{\frac{1}{21} + \frac{1}{14}} = 8.4$$

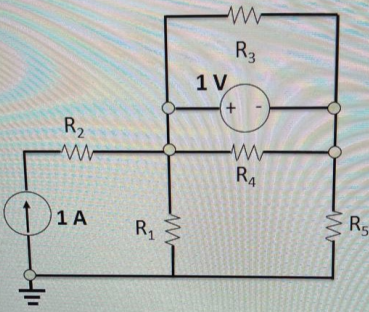
If resistors = 13 Ω ,
 $R_{eq1} = 6.5$

$$R_{eq2} = R_{eq1} + R_3 = 19.5$$

$$R_{eq2} // R_2 = 7.8$$

Question 5

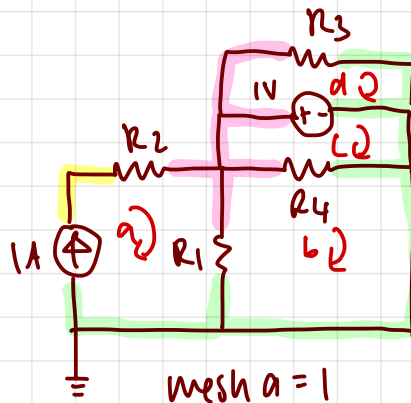
In the circuit below, what is the Norton (short-circuit) current when R_5 is the load?



Given $R_1 = 2\ \Omega$, $R_2 = 1\ \Omega$, $R_3 = 2\ \Omega$, $R_4 = 3\ \Omega$, $R_5 = 4\ \Omega$

Which among the following values most closely matches the correct answer?

- ☐ a. 0.6 A
- ☐ b. 0.5 A
- ☐ c. 0.7 A
- ☐ d. 0.8 A



$$\text{mesh a} = 1$$

$$\text{mesh b} = R_1(i_b - i_a) + R_4(i_b - i_c) = 0$$

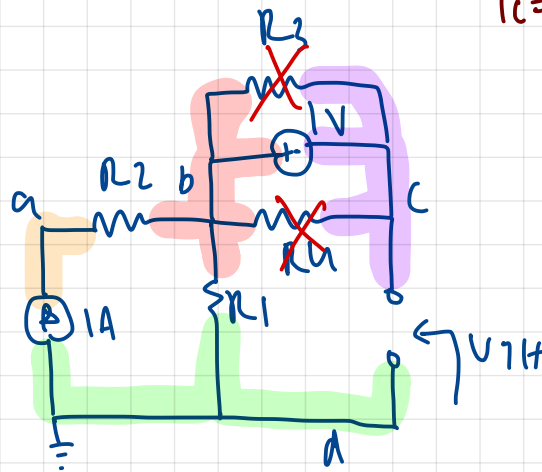
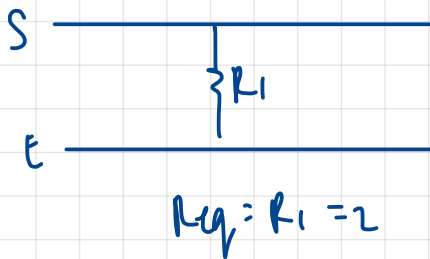
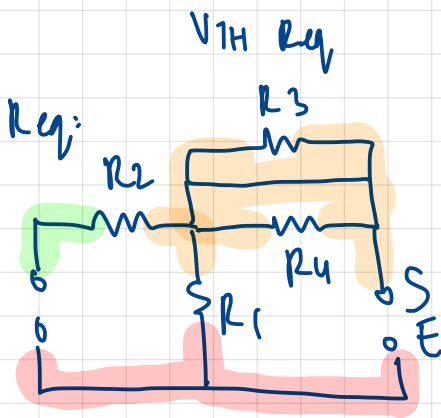
$$2i_b - 2 + 3i_b - 3i_c = 0$$

$$5i_b - 3i_c = 2$$

$$\text{mesh c} = R_4(i_c - i_b) = -1$$

$$3(i_c - i_b) = -1$$

$$i_c = \frac{1}{6} \quad i_b = \frac{1}{2}$$



$$V_b = (2)(1) = 2$$

$$V_b - V_c = 1$$

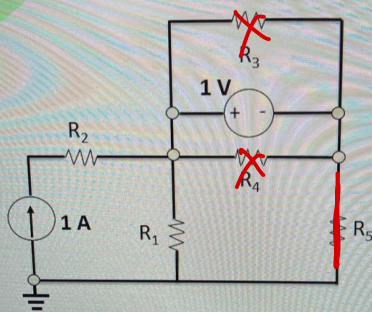
$$2 - V_c = 1$$

$$V_c = 1$$

$$\therefore V = \frac{1}{2}$$

Question 5

In the circuit below, what is the Norton (short-circuit) current when R_5 is the load?

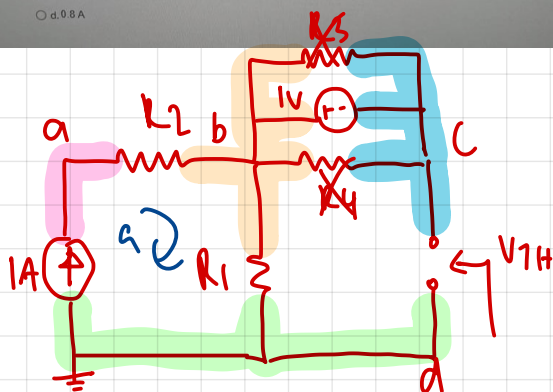


$$\begin{aligned} 4(1b-1a) + 1 &= 0 \\ 2(1b-1) + 1 &= 0 \\ 21b &= -1 + 2 \\ 1b &= 0.5 \text{ A} \end{aligned}$$

Given $R_1 = 2 \Omega$, $R_2 = 1 \Omega$, $R_3 = 2 \Omega$, $R_4 = 3 \Omega$, $R_5 = 4 \Omega$

Which among the following values most closely matches the correct answer?

- ☐ a. 0.6 A
☒ b. 0.5 A
☐ c. 0.7 A
☐ d. 0.8 A



current? $V = IR$

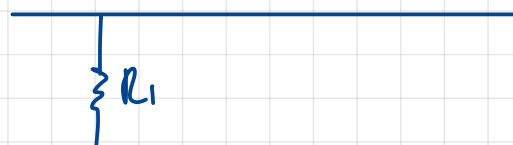
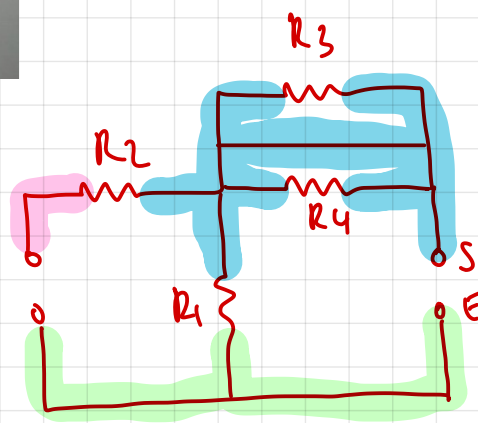
mesh $a = 1A$

$$V_b = (1)(2) = 2V$$

$$V_b - V_c = 1$$

$$2 - V_c = 1$$

$$\begin{aligned} I &= \frac{V}{R} \\ &= \frac{1}{2} \\ &= 0.5 \end{aligned}$$

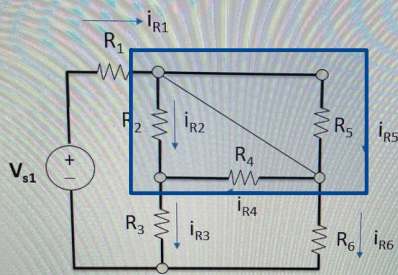


$$R_{eq} = R_1 = 2$$

⏪ ⚠ Moving to the next question prevents changes to this answer.

Question 3

What's the current in R_3 , i.e., i_{R3} , in the following circuit? (Hint: use supernode)



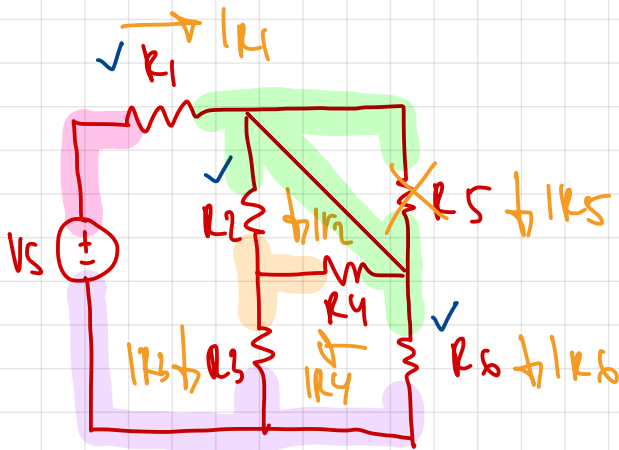
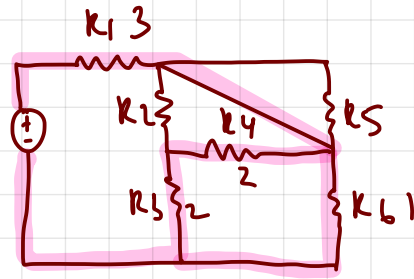
$$\begin{aligned} I_n &= \text{out} \\ I_1 &= I_{R3} + I_{R6} \\ 3 &= I_{R3} + 1 \\ I_{R3} &= 2 \end{aligned}$$

Given $i_{R1} = 3\text{ A}$, $i_{R2} = 2\text{ A}$, $i_{R6} = 1\text{ A}$

Which among the following values most closely matches the correct answer?

- ☐ a. 1.0 A
- ☐ b. 1.5 A
- ☐ c. 0.5 A
- ☒ d. 2.0 A

⏪ ⚠ Moving to the next question prevents changes to this answer.

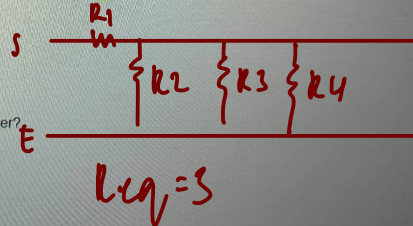
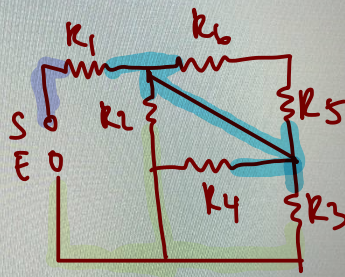
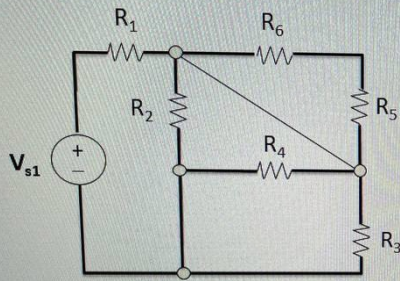


$$\begin{aligned} I_{R1} &= 3\text{ A} \\ I_{R2} &= 2\text{ A} \\ I_{R6} &= 1\text{ A} \end{aligned}$$

node voltage method

$$I_{R1}$$

What's the equivalent resistance seen by V_{s1} in the following circuit? (Hint: label different node with different color)

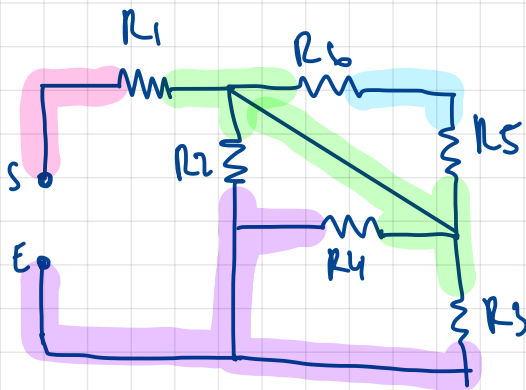


Given $R_1 = 2\ \Omega$, $R_2 = 3\ \Omega$, $R_3 = 3\ \Omega$, $R_4 = 3\ \Omega$, $R_5 = 1\ \Omega$, $R_6 = 2\ \Omega$

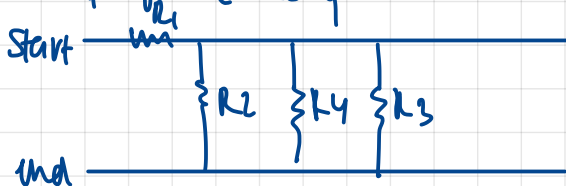
Which among the following values most closely matches the correct answer?

- ☐ a. $4\ \Omega$
- ☐ b. $1\ \Omega$
- ☒ c. $3\ \Omega$
- ☐ d. $2\ \Omega$

Moving to the next question prevents changes to this answer.



* Ignore R_5 & R_6 :

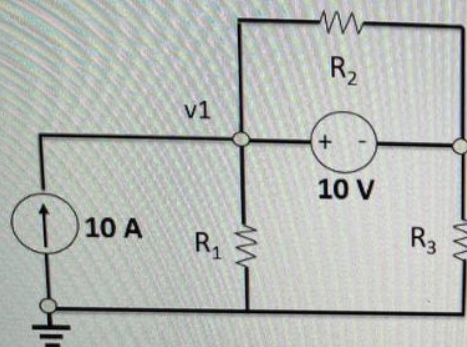


$$R_2 || R_3 || R_4 = \frac{1}{\frac{1}{3} + \frac{1}{3} + \frac{1}{3}} = 1$$

$$R_1 + R_{eq} = 3\ \Omega$$

Question 2

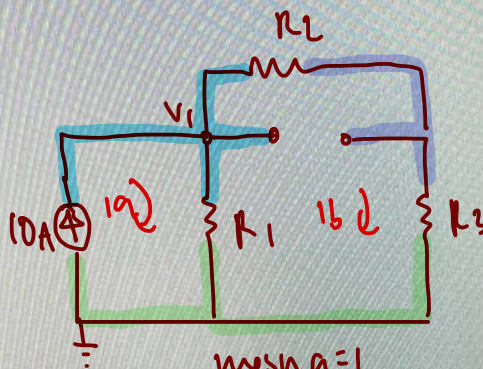
In the circuit below, what is the Thevenin (open-circuit) voltage when the voltage source is the load?



Given $R_1 = R_2 = R_3 = 1.5 \Omega$

Which among the following values most closely matches the correct answer?

- ☒ a. 5 V
- ☐ b. 8 V
- ☐ c. 7 V
- ☐ d. 6 V



mesh a = 1

$$\text{mesh b} = R_1(i_2 - i_1) + R_3(i_2) + 10(i_2) = 0$$

$$1.5(i_2 - 10) + 1.5i_2 + 1.5i_2 = 0$$

$$4.5i_2 = 15$$

$$i_2 = 3.3333$$

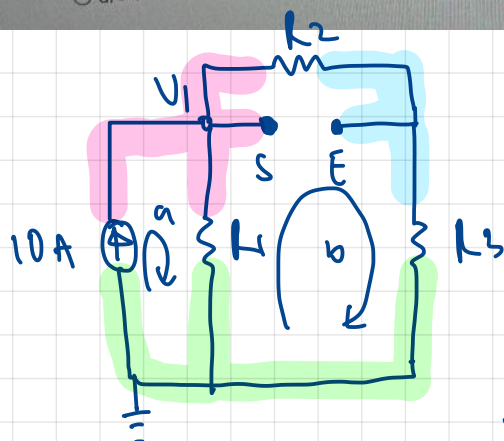
$$V_1 = (10 - 3.3333)(1.5) = 10$$

$$V_1 - V_3 = V_{TH}$$

$$3.3333 \times 1.5 = 5$$

$$10 - 5 = V_{TH}$$

$$V_{TH} = 5$$



$$V = 10$$

mesh b

$$(i_2 - i_1)R_1 + i_2R_2 + i_2R_3 = 0$$

$$(i_2 - 10)(1.5) + i_2(1.5) + i_2(1.5) = 0$$

$$i_2 - 10 + i_2 + i_2 = 0$$

$$3i_2 - 10 = 0$$

$$\text{mesh a} = 10$$

$$3i_2 - 10 = 0$$

$$i_2 = \frac{10}{3}$$

$$V_3 = 10$$

$$= \frac{10}{3} (1.5) = 5$$

$$V_1 = 10$$

$$= (10 - \frac{10}{3})(1.5)$$

$$= 10$$

$$V_1 - V_2 = V_{TH}$$

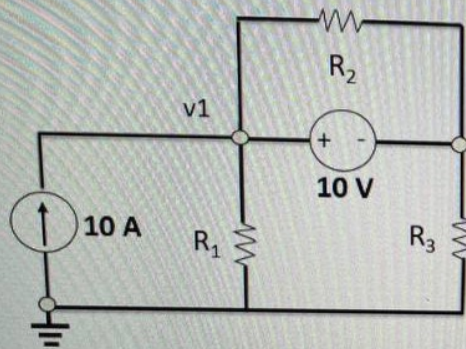
$$10 - 5 = V_{TH}$$

$$V_{TH} = 5$$

Question 2

video

In the circuit below, what is the Thevenin (open-circuit) voltage when the voltage source is the load?

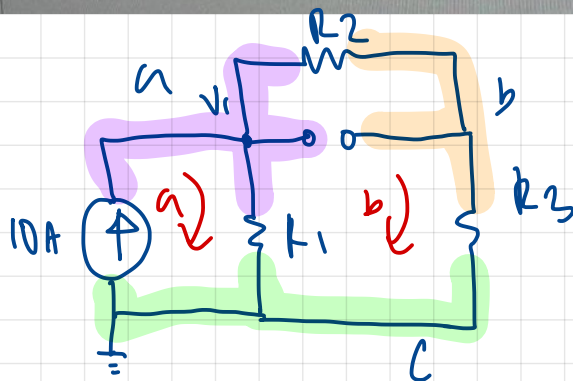


Given $R_1 = R_2 = R_3 = 1.5 \Omega$

Which among the following values most closely matches the correct answer?

- ☒ a. 5 V
- ☐ b. 8 V
- ☐ c. 7 V
- ☐ d. 6 V

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$$V_{TH} = V_a - V_b$$

$$V_a = 10$$

$$V_b = (1b - 1a)R_1 + 1b(R_2) + 1b(R_3) = 0$$

$$(1b - 1a)1.5 + 1b(1.5) + 1b(1.5) = 0$$

$$31b - 1a = 0$$

$$31b - 10 = 0$$

$$1b = \frac{10}{3}$$

$$V_3 = \frac{10}{3} (1.5) = 5$$

$$V_1 = \left(10 - \frac{10}{3}\right) (1.5)$$

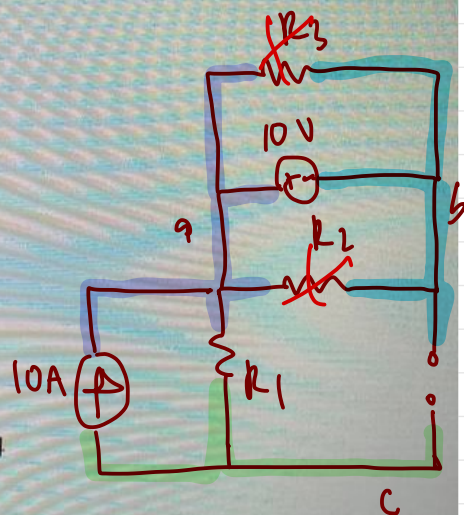
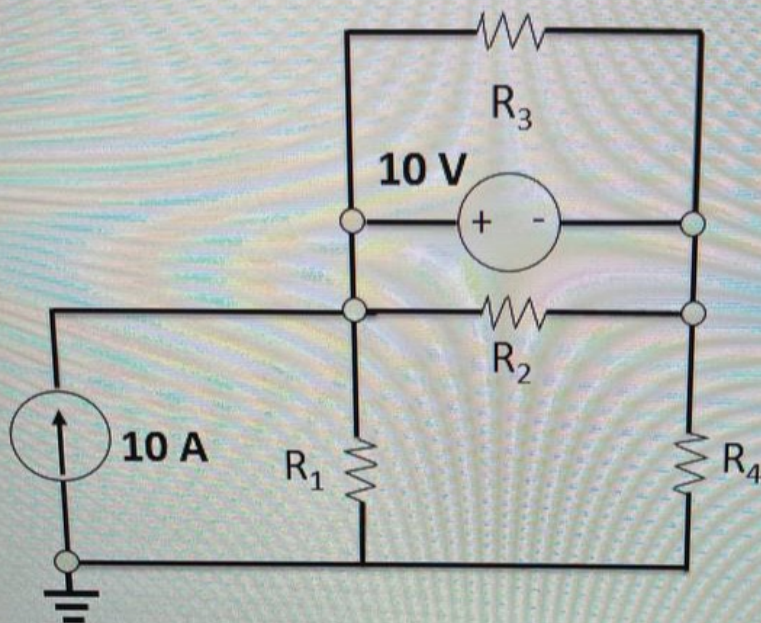
$$= 10$$

$$V_a - V_b = V_{TH}$$

$$10 - 5 = V_{TH}$$

$$V_{TH} = 5$$

In the circuit below, what is the Thevenin (open-circuit) voltage when R_4 is the load?



$$V_a = (10)(7.5) = 75$$

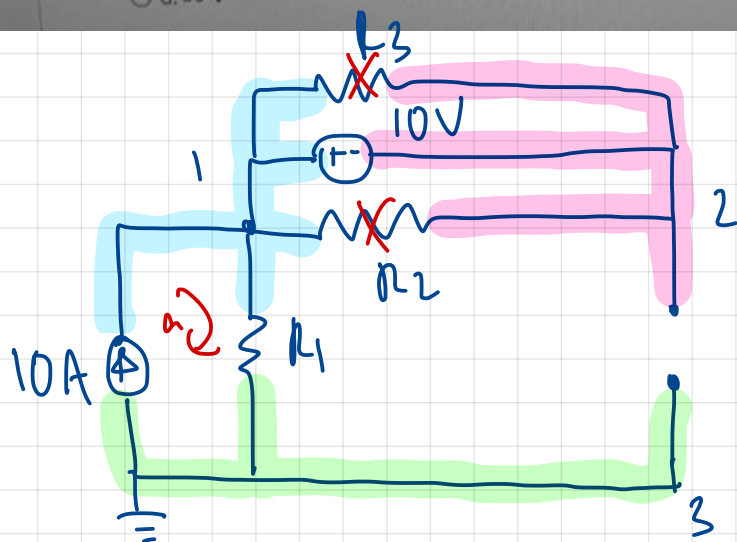
$$75 - V_b = 10$$

$$V_b = 65$$

Given $R_1 = R_2 = R_3 = R_4 = 7.5 \Omega$

Which among the following values most closely matches the correct answer?

- ☐ a. 60 V
- ☒ b. 65 V
- ☐ c. 45 V
- ☐ d. 30 V



$$V = 10$$

$$\text{mesh A} = 10A$$

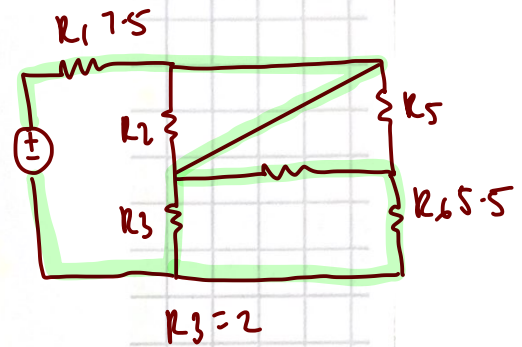
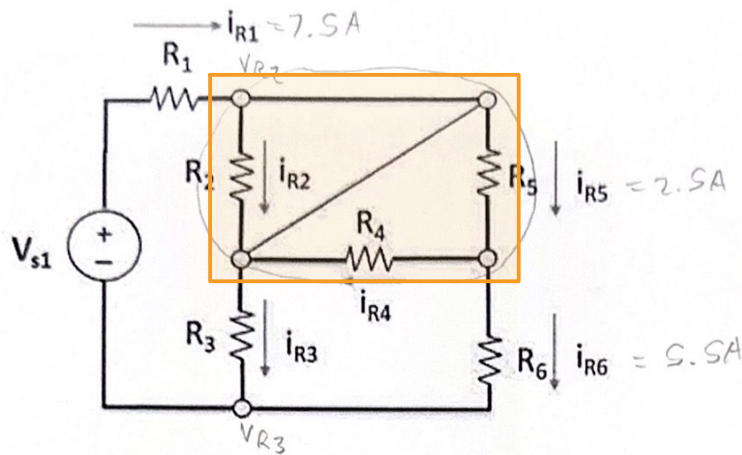
$$V_1 = (10)(7.5)$$

$$= 75$$

$$75 - 10 = V_2$$

$$V_2 = 65$$

What's the current in R_3 , i.e., i_{R3} , in the following circuit? (Hint: use supernode)



Given $i_{R1} = 7.5A$, $i_{R5} = 2.5A$, $i_{R6} = 5.5A$

Which among the following values most closely matches the correct answer?

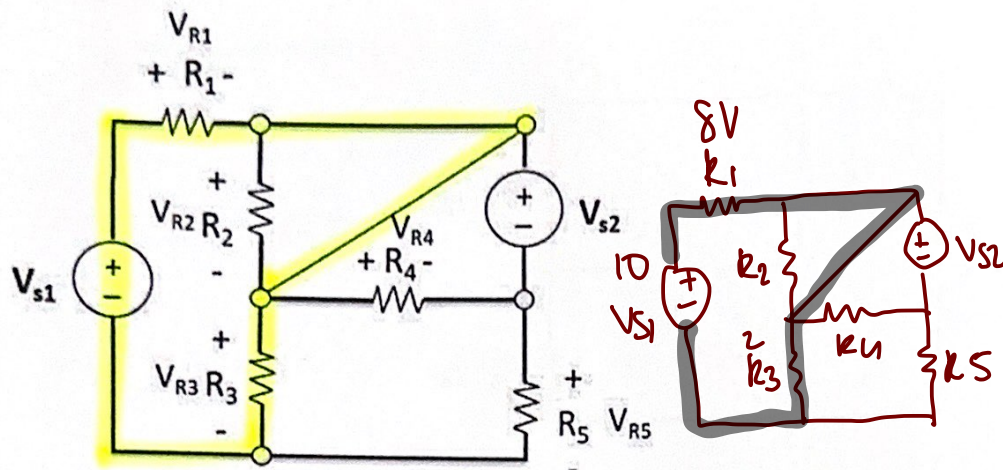
- ☐ a. 2.5A
- ☐ b. 3.0A
- ☒ c. 2.0A
- ☐ d. 1.5A

KCL of supernode: current in = current out
 $i_{R1} = i_{R3} + i_{R6}$
 $7.5A = i_{R3} + 5.5A$
 $i_{R3} = 2A$

Ans: 2A

$$\begin{aligned} i_{R1} &= i_{R3} + i_{R6} \\ 7.5 &= i_{R3} + 5.5 \\ i_{R3} &= 2 \end{aligned}$$

What's the voltage across R_3 , i.e., V_{R3} , in the following circuit? (Hint: label different node with different color)



Given $V_{R1} = 8V$, $V_{R5} = 1V$, $V_{S1} = 10V$, and $V_{S2} = 1V$

Which among the following values most closely matches the correct answer?

- ☐ a. 1V
- ☐ b. 3V
- ☐ c. 4V
- ☒ d. 2V

KVL of highlighted loop:

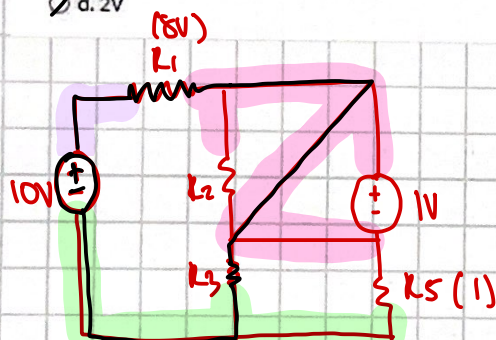
$$V_{S1} - V_{R1} - V_{R3} = 0$$

$$10 - 8 - V_{R3} = 0$$

$$2 - V_{R3} = 0$$

$$V_{R3} = 2V //$$

Ans: 2V //



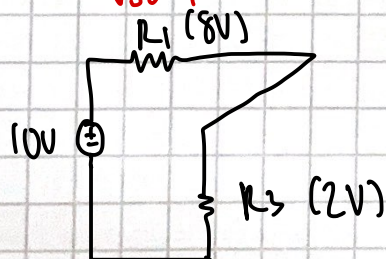
$$V_{R1} = 8V$$

$$V_{R5} = 1$$

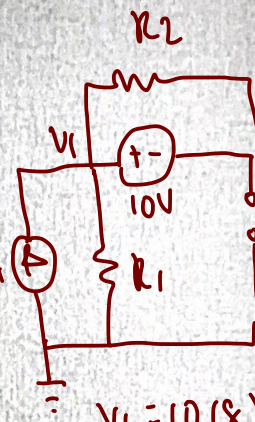
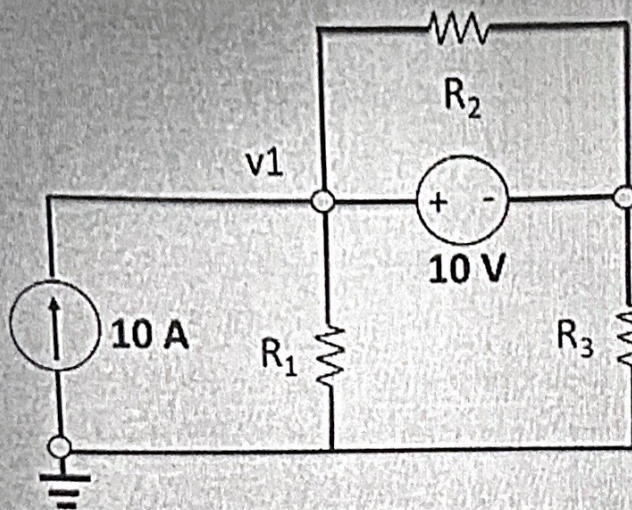
$$V_{S1} = 10$$

$$V_{S2} = 1$$

* ignore V_{S2} & R_2



In the circuit below, what is the Thevenin (open-circuit) voltage when R_3 is the load?



$$V_1 = 10(8) = 80$$

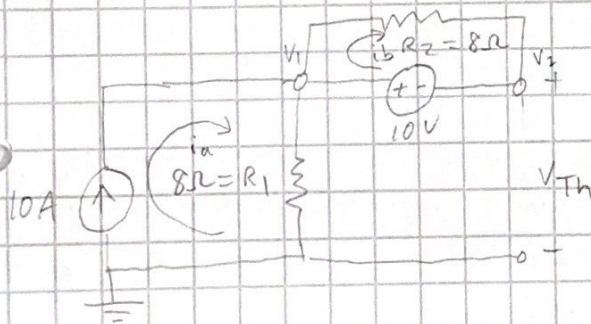
$$80 - V_{TH} = 10$$

$$V_{TH} = 70V$$

Given $R_1 = R_2 = R_3 = 8 \Omega$

Which among the following values most closely matches the correct answer?

- ☐ a. 65V
- ☐ b. 75V
- ☐ c. 60V
- ☒ d. 70V



KVL at (a)

$$I_a = 10A$$

KVL at (b)

$$I_b = \frac{10}{8} = 1.25A$$

$$\Delta V = I R_1$$

$$V_{TH} - 0 = I R_1$$

$$V_{TH} = 10 \times 8$$

$$= 80V$$

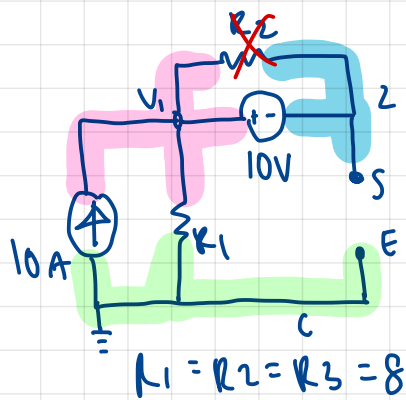
$$V_1 - V_2 = 10V$$

$$V_{TH} - V_2 = 10$$

$$80 - V_2 = 10$$

$$V_2 = 70V$$

Ans: 70V //



$$V = IR$$

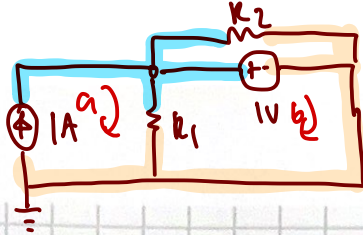
$$= (10)(8) = 80$$

$$V_1 - V_2 = 10$$

$$80 - V_2 = 10$$

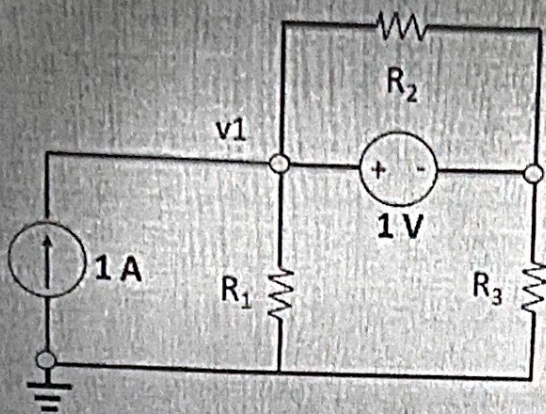
$$-V_2 = -70$$

$$V_2 = 70$$



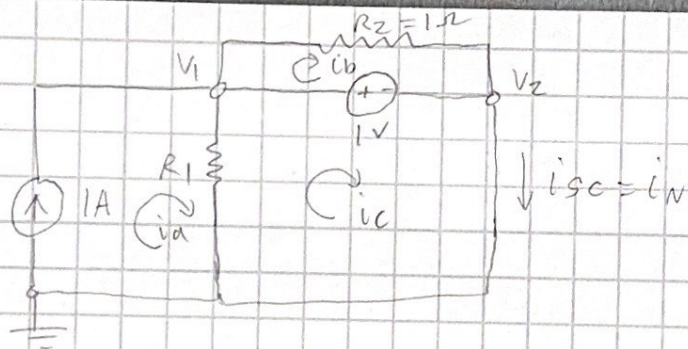
$\text{mesh } a = 1$
 $\text{mesh } b = (i_b - i_a)R_1 = -1$
 $2.5i_b - 2.5 = -1$
 $i_b = 0.6$

In the circuit below, what is the Norton (short-circuit) current when R_3 is the load?



Given $R_1 = 2.5 \Omega$, $R_2 = 1 \Omega$ Which among the following values most closely matches the correct answer?

- ☐ a. 0.8A
- ☐ b. 0.5A
- ☒ c. 0.6A
- ☐ d. 0.7A



KVL at (a):

$$i_a = 1A$$

KVL at (b):

$$i_b = 1A$$

KVL at c:

$$-(i_c - i_a)2.5 - 1 = 0$$

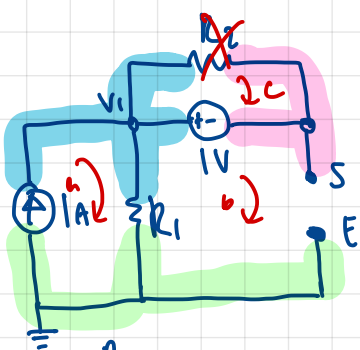
$$-2.5i_c + 2.5(1) - 1 = 0$$

$$-2.5i_c + 1.5 = 0$$

$$i_c = 0.6A$$

$$i_{sc} = i_c = 0.6A$$

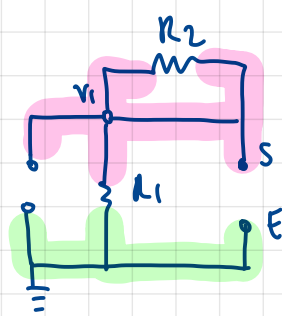
Ans: 0.6A



$$R_1 = 2.5 \Omega$$

$$R_2 = 1 \Omega$$

$$V = 1K$$



$$R_{eq} = R_1 = 2.5$$

$$V_{TH} =$$

using mesh current method,

$$\text{mesh A} = 1$$

$$\text{mesh B} = X$$

$$\text{mesh C} = 1 = (i_c)(R_2)$$

$$i_c = 1$$

$$V_1: V = (1)(2.5) = 2.5$$

$$V_1: V_1 - V_2 = 1$$

$$2.5 - V_2 = 1$$

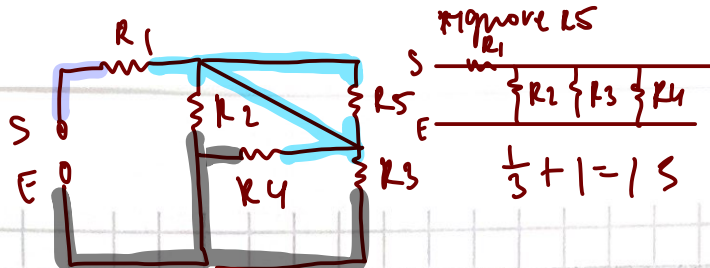
$$V_2 = 1.5$$

$$\therefore V = 1K$$

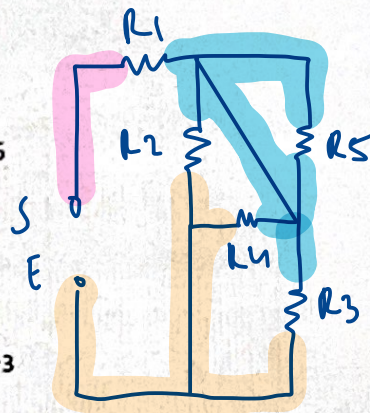
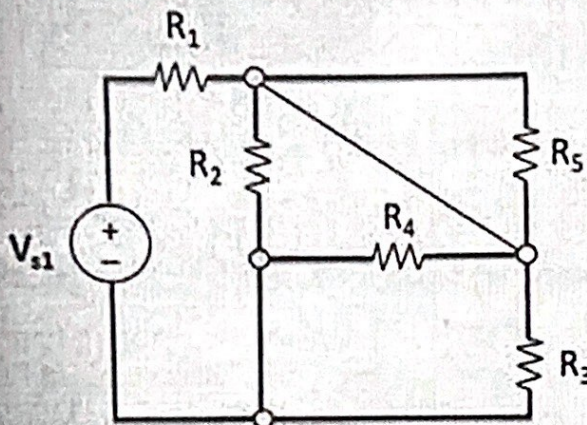
$$1.5 = 1(2.5)$$

$$1 = 0.6$$

~~A~~



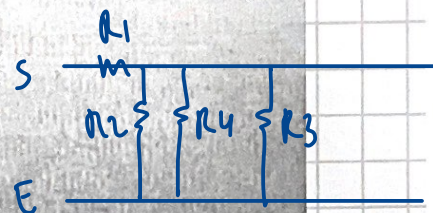
What's the equivalent resistance seen by V_{s1} in the following circuit?
(Hint: label different node with different color)



Given $R_1 = 1 \Omega$, $R_2 = 1 \Omega$, $R_3 = 1 \Omega$, $R_4 = 1 \Omega$, $R_5 = 2 \Omega$

Which among the following values most closely matches the correct answer?

- ☒ a. 1.3Ω
- ☐ b. 2.6Ω
- ☐ c. 3.6Ω
- ☐ d. 1.6Ω



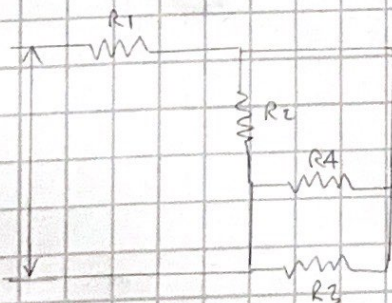
$$R_T = (R_3 \parallel R_4 + R_5) \parallel R_2 + R_1$$

$$= 1.714 \Omega$$

$$R_2 \parallel R_4 \parallel R_3 = \frac{1}{3}$$

$$\frac{1}{3} + 1 = 1.3$$

$R_5 \Rightarrow \text{Short}$



$$R_{34} = R_3 \parallel R_4 = \left(\frac{1}{1} + \frac{1}{1} \right)^{-1} = \frac{1}{2} \Omega$$

$$R_{234} = R_2 \parallel R_{34} = \left(\frac{1}{\frac{1}{2}} + \frac{1}{1} \right)^{-1} = \frac{1}{3} \Omega$$

$$R_1 + R_{234} = 1 + \frac{1}{3} \Omega$$

$$= 1.3 \Omega //$$

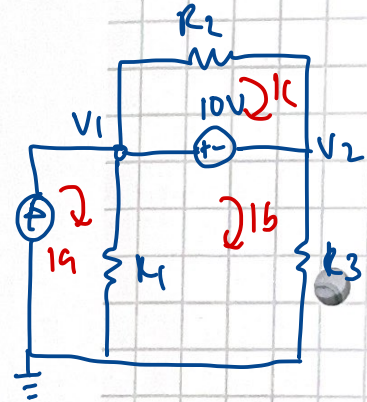
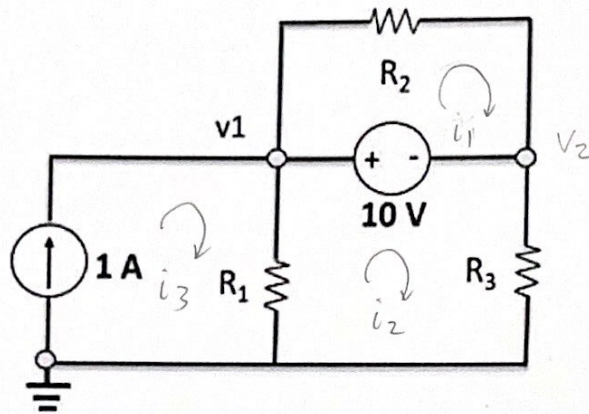
Ans: 1.3Ω

Question 1



In the circuit below, what is the node voltage v_1 ?

Given $R_1 = R_2 = R_3 = 110 \Omega$



Mesh $a = 1A$

Mesh $b = R_1(i_b - 1) + R_3(i_b) = -10$

$$110i_b - 110 + 110i_b = -10$$

$$220i_b = 100$$

$$i_b = 0.4545$$

$$v_2 = (0.4545)(110) = 50$$

$$v_1 - v_2 = 10$$

$$v_1 - 50 = 10$$

$$v_1 = 60V$$

$$R_2 i_1 + 10 = 0 \rightarrow i_1 = \frac{1}{11}$$

$$-10 + R_3 i_2 + R_1(i_2 - 1) = 0$$

$$-10 + i_2(R_3 + R_1) - R_1 = 0 \rightarrow i_2 = \frac{6}{11}$$

Since node on R_3 = node on R_1 ,

$$i_2 R_3 = v_1$$

$$v_1 = \frac{6}{11}(110)$$

$$= 60$$

$$-R_2 i_1 - 10 = 0$$

$$-R_2 i_1 = -10$$

$$i_1 = \frac{1}{11}$$

$$-R_3 i_2 - R_1(i_2 - 1) + 10 = 0$$

$$-R_3 i_2 - R_1 i_2 + R_1 + 10 = 0$$

$$-i_2(R_3 + R_1) + R_1 + 10 = 0$$

$$-i_2(110 + 110) + 110 + 10 = 0$$

$$-220i_2 + 120 = 0$$

$$i_2 = \frac{6}{11}$$

$$v_1 = i_2 R_3$$

$$= \frac{6}{11}(110)$$

$$= 60V$$

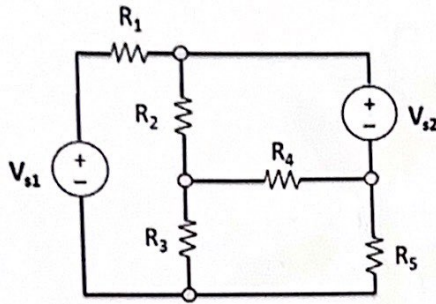
Ans: 60V

Question 2



What's the equivalent resistance seen by R_4 in the following circuit? (Hint: short circuit V_{s1} and V_{s2})

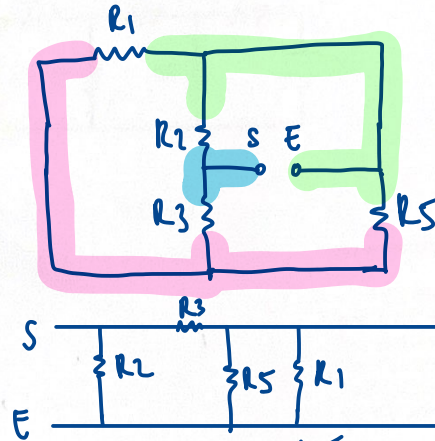
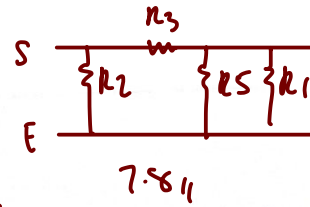
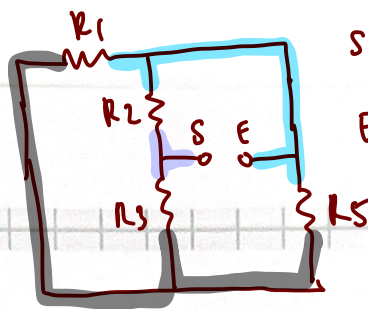
Given $R_1 = R_2 = R_3 = R_4 = R_5 = 13 \Omega$



Selected Answer: ☒ 7.8 Ω

- Answers:
- ☐ 6.8 Ω
 - ☒ 7.8 Ω
 - ☐ 9.8 Ω
 - ☐ 8.8 Ω

$$R_1 = [(R_1 \parallel R_5) + R_2] \parallel R_3 = 7.8 \Omega$$



$$R_{eq1} = R_1 \parallel R_5 = 6.5$$

$$R_{eq2} = R_{eq1} + R_3 = 19.5$$

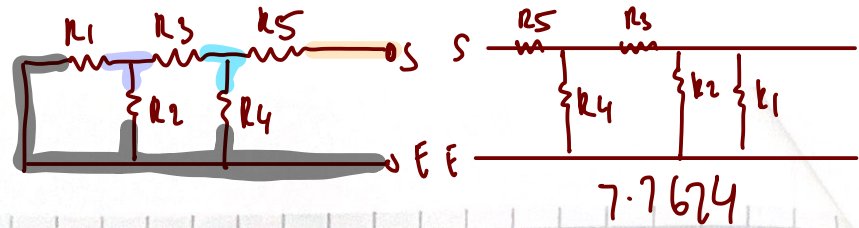
$$R_{eq2} \parallel R_4 = 7.8$$

$$R_{12} = R_1 \parallel R_2 = 6.5 \Omega$$

$$R_{12} + R_3 = 19.5$$

$$(R_{12} + R_3) \parallel R_5 = 7.8 \Omega$$

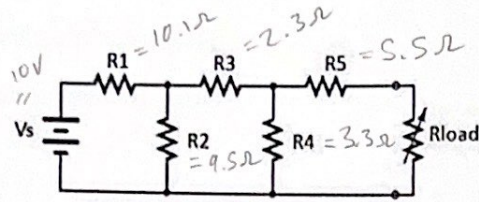
Ans: 7.8 Ω



Question 3



Referring to the following circuit



and knowing that

$V_s = 10 \text{ [V]}$
 $R_1 = 10.1 \text{ [Ohms]}$
 $R_2 = 9.5 \text{ [Ohms]}$
 $R_3 = 2.3 \text{ [Ohms]}$
 $R_4 = 3.3 \text{ [Ohms]}$
 $R_5 = 5.5 \text{ [Ohms]}$

$$R_1 // R_2 = 4.895 \Omega$$

$$(R_1 // R_2) + R_3 = 7.195 \Omega$$

$$((R_1 // R_2) + R_3) // R_4 = 2.262 \Omega$$

$$(((R_1 // R_2) + R_3) // R_4) + R_5 = 7.762 \Omega$$

$\downarrow$
 R_{load}

determine the value of R_{load} which ensures maximum power transfer.

Allowing for some numerical approximation, which among the following values most closely matches the correct answer?

Selected Answer: ☒ $R_{load} = 7.7624 \text{ [Ohms]}$

Answers: ☐ $R_{load} = 15.5248 \text{ [Ohms]}$

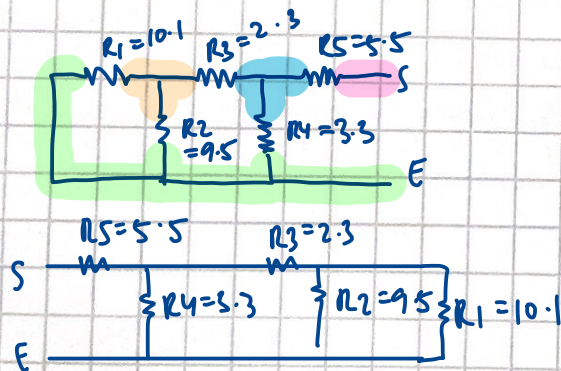
☐ $R_{load} = -2.2376 \text{ [Ohms]}$

☒ $R_{load} = 7.7624 \text{ [Ohms]}$

☐ $R_{load} = 30.7 \text{ [Ohms]}$

$$R_1 = [(R_1 // R_2) + R_3] // R_4 + R_5$$

$$= 7.7624 \Omega$$



$$R_{eq1} = R_1 // R_2 = 4.8954$$

$$R_{eq2} = R_{eq1} + R_3 = 7.1954$$

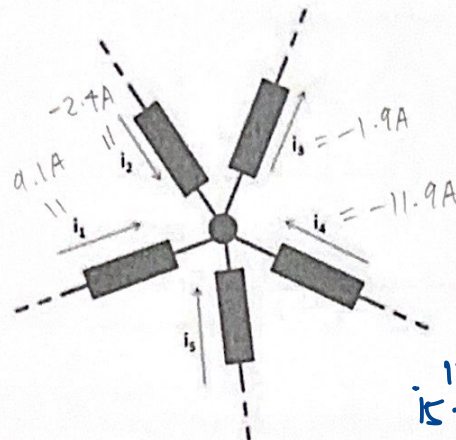
$$R_{eq3} = 7.1954 // R_4 = 2.2624$$

$$R_{eq3} + R_5 = 7.7624 \Omega$$

Question 4



Referring to the following circuit



$$I_{in} = I_{out}$$

$$12.1 + 1.5 + 1.4 = 15$$

$$15 = 3.3$$

$$I_{in} = I_{out}$$

$$15 - 11.9 - 2.4 + 9.1 = 1.9$$

$$i_5 = 3.3$$

and knowing that

- $i_1 = 9.1 \text{ [A]}$
- $i_2 = -2.4 \text{ [A]}$
- $i_3 = -1.9 \text{ [A]}$
- $i_4 = -11.9 \text{ [A]}$

$$i_5 + i_1 + i_2 + i_4 = i_3$$

$$i_5 + 9.1 + (-2.4) + (-11.9) = -1.9$$

$$i_5 - 5.2 = -1.9$$

$$i_5 = 3.3 \text{ A}$$

determine the value of i_5 .

Allowing for some numerical approximation, which among the following values most closely matches the correct answer?

Selected Answer: ☒ $i_5 = 3.3 \text{ A}$

- Answers:
- ☐ $i_5 = -3.3 \text{ A}$
 - ☐ $i_5 = -1.3 \text{ A}$
 - ☐ $i_5 = 0.3 \text{ A}$
 - ☒ $i_5 = 3.3 \text{ A}$

$$i_1 + i_2 + i_4 + i_5 = i_3$$

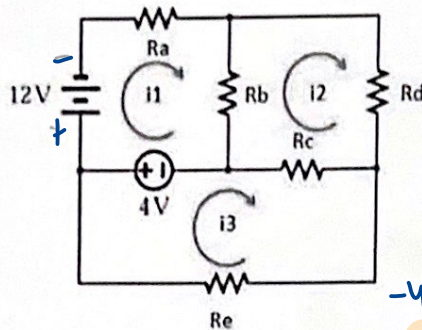
$$i_5 = i_3 - i_1 - i_2 - i_4$$

$$= 3.3 \text{ A}$$

Question 5



The mesh-current method, applied to the following circuit



$$V=12$$

mesh a:

$$-8 = 3.1i_1 + (i_1 - i_2)4.5$$

mesh b:

$$(i_2 - i_1)4.5 + 20.3(i_2) + (i_2 - i_3)(20.2) = 0$$

mesh c:

$$-4 = (i_3 - i_2)20.2 + (i_3)(15.5)$$

$$(3.1 + 4.5)i_1 - 4.5i_2 = -8$$

$$7.6i_1 - 4.5i_2 = -8$$

$$-4.5i_1 + (4.5 + 20.3 + 20.2)i_2 - 20.2i_3 = 0$$

$$-4.5i_1 + 45i_2 - 20.2i_3 = 0$$

$$-20.2i_2 + 35.7i_3 = -4$$

mesh 1:

$$-8 = R_a(i_1) + R_b(i_1 - i_2)$$

$$7.6i_1 - 4.5i_2 = -8$$

mesh 2:

$$R_b(i_2 - i_1) + R_c(i_2 - i_3) + R_d(i_2) = 0$$

$$-4.5i_1 + 45i_2 - 20.2i_3 = 0$$

mesh 3:

$$-4 = R_c(i_3 - i_2) + R_e(i_3)$$

$$-20.2i_2 + 35.7i_3 = -4$$

will lead to a 3x3 system of equations such as

$$\begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix} \cdot \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix} = \begin{bmatrix} -8V \\ 0V \\ -4V \end{bmatrix}$$

Allowing for some numerical approximation and knowing

$R_a = 3.1$ [Ohms]
 $R_b = 4.5$ [Ohms]
 $R_c = 20.2$ [Ohms]
 $R_d = 20.3$ [Ohms]
 $R_e = 15.5$ [Ohms]

$$7.6i_1 - 4.5i_2 = -8 \quad (1)$$

$$-4.5i_1 + 45i_2 - 20.2i_3 = 0 \quad (2)$$

$$-20.2i_2 + 35.7i_3 = -4 \quad (3)$$

which among the following matrices best represents the resistance matrix $[R_{ij}]$ in the equation above?

Selected Answer:

$$\begin{bmatrix} 7.6 & -4.5 & 0 \\ -4.5 & 45 & -20.2 \\ 0 & -20.2 & 35.7 \end{bmatrix}$$

$$12V + i_1R_a + (i_1 - i_2)R_b - 4V = 0$$

$$i_1(R_a + R_b) - R_b i_2 = -8V$$

Answers:

$$\begin{bmatrix} 7.6 & 0 & 0 \\ 0 & 45 & 0 \\ 0 & 0 & 35.7 \end{bmatrix}$$

$$(i_2 - i_1)R_b + i_2R_d + (i_3 - i_2)R_c = 0$$

$$-R_b i_1 + i_2(R_b + R_d + R_c) - R_c i_3 = 0$$

$$\begin{bmatrix} 7.6 & -4.5 & -20.2 \\ 0 & 45 & 40.6 \\ 0 & 0 & 35.7 \end{bmatrix}$$

$$4V + (i_3 - i_2)R_c + i_3R_e = 0$$

$$-R_c i_2 + i_3(R_c + R_e) = -4V$$

$$\begin{bmatrix} 3.1 & 4.5 & 20.2 \\ 4.5 & 20.3 & 15.5 \\ 20.2 & 15.5 & 18.6 \end{bmatrix}$$

$$\begin{bmatrix} 7.6 & -4.5 & 0 \\ -4.5 & 45 & -20.2 \\ 0 & -20.2 & 35.7 \end{bmatrix}$$